## Reasoning and Problem Solving Step 7: Lengths and Angles in Shapes

## National Curriculum Objectives:

Mathematics Year 5: (5G2a) Use the properties of rectangles to deduce related facts and find missing lengths and angles
Mathematics Year 5: (5G4b) Identify: angles at a point and one whole łurn (total 360), angles at a point on a straight line and $1 / 2$ a turn (total 180) other multiples of $90^{\circ}$

## Differentiation:

Questions 1, 4 and 7 (Reasoning)
Developing Use knowledge of angles in shapes, including squares, rectangles and 6 sided rectilinear compound shapes, to explain if a given angle is correct or not.
Expected Use knowledge of angles in shapes, including triangles, squares, rectangles and 6 sided rectilinear compound shapes, to explain if a given angle is correct or not.
Questions using adjoining shapes.
Greater Depth Use knowledge of angles in shapes, including triangles, quadrilaterals and 8 sided rectilinear compound shapes, to explain if a given angle is correct or not. More than one adjoining shape per question.

Questions 2, 5 and 8 (Problem Solving)
Developing Use clues about the properties of a shape, including squares, rectangles and 6 sided rectilinear compound shapes to determine the possible length of the sides. Expected Use clues about the properties of a shape, including triangles, squares, rectangles and 6 sided rectilinear compound shapes, to determine the length of the sides. Greater Depth Use clues about the properties of a shape, including triangles, quadrilaterals and 8 sided rectilinear compound shapes to determine the length of the sides or the angles within.

Questions 3, 6 and 9 (Reasoning)
Developing Given two statements about the properties of shapes, including squares, rectangles and 6 sided rectilinear compound shapes, determine which is correct, including angles of $90^{\circ}$ and $45^{\circ}$.
Expected Given two statements about the properties of shapes, including triangles, squares, rectangles and 6 sided rectilinear compound shapes, determine which is correct, including any angles.
Greater Depth Given two always, sometimes, never statements about the properties of shapes, including triangles, quadrilaterals and 8 sided rectilinear compound shape, determine which is correct.

## More Year 5 Properties of Shapes resources.

Did you like this resource? Don't forget to review it on our website.

1a. Jack thinks he has picked the correct degrees for angle $A$.


Do you agree? Explain why.

2a. Arron has a rectangle with a perimeter of 26 cm .


What length is each side? Give 3 possible answers.

3a. Elvis and Willow are discussing the properties of a shape.


1b. Lizzy thinks she has picked the correct degrees for angle A.


Do you agree? Explain why.

2b. Rhonda has a square with a perimeter less than 50cm.


What length is each side? Give 3 possible answers.

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3b. April and Charlie are discussing right angles in a shape.


4a. Lola thinks she has picked the correct degrees for the total of angle $A$ and angle


Do you agree? Explain why.

5a. Jack has a rectangle with a perimeter between 20 cm and 30 cm . Sides $A$ and $C$ are 4 cm longer than sides $B$ and $D$.


What length is each side? Give 3 possible answers.

6a. Sophie and Will are calculating angles in a shape.


4b. Alfie thinks he has picked the correct degrees for angle $A$.


Do you agree? Explain why.

5b. Mia has a rectangle with a perimeter between 30 cm and 40 cm . Sides B and D are 5 cm shorter than sides $A$ and $C$.


What length is each side? Give 3 possible answers.

6b. Niko and Sara are calculating angles in a shape.


7a. Liam thinks he has picked the correct degrees for angle $A$.


Do you agree? Explain why.

8a. Bridget has a triangle with a perimeter of between 15 cm and 30 cm . Side $A$ is 2 cm longer than side $B$. Side $B$ is 5 cm longer than side $C$.


B
What length is each side? Give 3 possible answers.

9a. Jordan and Tia are calculating angles in a shape.


Who is correct? Why?
Tia

7b. Nadia thinks she has picked the correct degrees for angle A.


Do you agree? Explain why.

8b. Josef is calculating the angles in a triangle. He knows that the second angle is twice as big as the first and the third angle is three times as big as the first.


What are the three angles? Is there more than one answer?

9b. Mina and Logan are calculating angles in a shape.


Who is correct? Why?
Logan

## Reasoning and Problem Solving Lengths and Angles in Shapes

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## Developing

1a. Jack is not correct because the angle is a combination of three $90^{\circ}$ angles, which is $270^{\circ}$.
2a. Various possible answers including; 7 cm and $6 \mathrm{~cm} ; 8 \mathrm{~cm}$ and $5 \mathrm{~cm} ; 9 \mathrm{~cm}$ and $4 \mathrm{~cm} ; 10 \mathrm{~cm}$ and $3 \mathrm{~cm} ; 11 \mathrm{~cm}$ and 2 cm ; or 12 cm and 1 cm .
3a. Elvis is correct as the shape will have four $45^{\circ}$ angles and 2 right angles:


## Expected

4 a . Lola is not correct because $90^{\circ}+45^{\circ}=$ $135^{\circ}$.
5a. Answers include: A and $\mathrm{C}=7 \mathrm{~cm}, \mathrm{~B}$ and $D=3 \mathrm{~cm} ; A$ and $C=8 \mathrm{~cm}, B$ and $D=$ $4 \mathrm{~cm} ; A$ and $C=9 \mathrm{~cm}, B$ and $D=5 \mathrm{~cm}$ 6 a. Will is correct as $180^{\circ}-87^{\circ}-36^{\circ}=57^{\circ}$.

## Greater Depth

7a. Liam is not correct because the internal angles of a triangle equal $180^{\circ}$. If one angles is $110^{\circ}$, the other is $35^{\circ}$, the third angle must be $35^{\circ}$.
8a. Answers include: $A=8 \mathrm{~cm}, B=6 \mathrm{~cm}$ and $C=1 \mathrm{~cm} ; A=10 \mathrm{~cm}, B=8 \mathrm{~cm}$ and $C=$ $3 \mathrm{~cm} ; A=12 \mathrm{~cm}, B=10 \mathrm{~cm}$ and $C=5 \mathrm{~cm}$.
9a. Tia is correct as a quadrilateral such as a square or rectangle has a right angle but other quadrilaterals have no right angles.

## Developing

1b. Lizzy is incorrect because the angle is a combination of a right angle and half a right angle, which is $135^{\circ}$.
2b. Various possible answers including; 1;
$2 ; 3 ; 4 ; 5 ; 6 ; 7 ; 8 ; 9 ; 10 ; 11$; or 12.
3b. Charlie is correct as a rectangle always has 4 right angles and 2 sets of parallel sides:


## Expected

4b. Alfie is not correct because the angle would only be $45^{\circ}$ if it cut through one square on the grid exactly.
5b. Answers include: $A$ and $C=10 \mathrm{~cm}, B$ and $D=5 \mathrm{~cm} ; A$ and $C=11 \mathrm{~cm}, B$ and $D=$ $6 \mathrm{~cm} ; A$ and $C=12 \mathrm{~cm}, B$ and $D=7 \mathrm{~cm}$
6b. Niko is correct, rectangles always have four $90^{\circ}$ angles. Sara's angles do not equal $360^{\circ}$.

## Greater Depth

7b. Nadia is correct because angles on a straight line $=180^{\circ}$. If one part of the angle is $115^{\circ}$, the other part must be $65^{\circ}$.
$8 \mathrm{~b} .30^{\circ}, 60^{\circ}$ and $90^{\circ}$. There is only one answer.
9b. Mina is correct as other angles could be calculated easily if it was a right angle, or if it was an isosceles or equilateral triangle, but if it was a scalene triangle, more information would be needed to calculate the other angles.

